QCD Physics and HERA - Lecture I

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- QCD Introduction.
- HERA Accelerator.
- Experiments.
- Deep Inelastic Scattering.
- Proton Structure.
- Photon Structure.
- α_S measurements.
- Beyond the SM.





The Strong Interaction I

- 4 fundamental Interactions: Weak, Electromagnetic, Gravity, Strong
- Strong interaction posited to account for cohesion of nuclei.
 - Must be strong (stronger than EM).
 - Must only be effective over short distances.
- Original Theory: Yukawa interaction (1935).
 - Model on QED.
 - Use a massive $\mathcal{O}(100 \text{ MeV})$ gauge boson to account for finite range.
 - Ideal candidate π discovered in cosmic ray + accelerator experiments in the 1940s.
 - Theorists made renormalisable field theories where nucleons interacted with each other via the exchange of pions, conserving isospin + strangeness.
- However perturbation expansions of QFTs of strong interaction broke down.

The Strong Interaction II

- In QED, succesive complicated diagrams for a process are suppressed by a factor $e^2 = \left(\frac{1}{137}\right)^2$ per loop. Meaning that only the simplest diagrams make an appreciable contribution to the total cross section.
- Strong interaction coupling g_S^2 was measured at around 15 for hadrons, so that extra loops make a very large contribution.
- Thus perturbative theories broke down, the first term could not be replied upon since its magnitude was so much smaller than subsequent terms.
- To make any prediction from theory one must sum the whole series, which is not possible.

Aces and Quarks

- In 1964 Gell-Mann and Zweig independently proposed that hadrons such as the proton were composite particles built from three basic blocks now known as up, down and strange.
- The proposed particles had very unusual properties:
 - $-spin \frac{1}{2}$ and baryon number $\frac{1}{3}$
 - -u and d form an isospin doublet with 0 strangeness.
 - -s an isospin 0 singlet with unit strangeness.
 - non-integral charge: $Q_u = +\frac{2}{3}$, $Q_{d,s} = -\frac{1}{3}$
- Mesons formed by $q\bar{q}$, nine combinations available, octet and singlet.
- Baryons formed by qqq, in SU(3) only decuplets, octets and singlets available.

ep scattering

- In the late 1960s a new phenomenon was observed at SLAC: scaling.
- SLAC used a 22 GeV linear electron accelerator.
- Accelerated electrons were scattered off protons and elastic *ep* scattering observed.
- Elastic *ep* scattering can be understood entirely in terms of *QED* as the exchange by proton and electron of a single photon. Electrons are structureless particles whereas protons are extended objects that should show structure.
- First measurements showed that cross sections at large angles in *ep* scattering were much smaller than in *ee* scattering.
 - Electrons seemed to act as 'hard' objects, bouncing off one another.
 - Protons seemed to be diffuse large objects that exerted a smaller impulse on passing particles.





Scaling in inelastic *ep* **scattering**

- Inelastic *ep* scattering was also thought to be mediated by single photon exchange between proton and electron, and it was thought that the most important process would be resonance production.
- analysis of the data at low electron scattering angle showed the expected behaviour.
- at large angles there remained a large measured cross section, despite the disappearance of individual resonance peaks.
- The inelastic *ep* cross section was behaving as though the proton contained: hard, point-like scattering centres.

Scaling in inelasic *ep* **scattering**

• In high energy *ep* scattering we can define the following variables:



• Structure functions F_1 and F_2 are defined in terms of the cross section:

$$\frac{d^2\sigma}{dxdQ^2} = \frac{4\pi\alpha^2}{Q^4} \{ [1 + (1-y)^2]F_1 + \frac{(1-y)}{x}(F_1 - 2xF_2) \}$$

• F_1 and F_2 are functions of x, Q^2 . Björken predicted that for $Q^2 \to \infty$, and x fixed the structure functions depend only on x.

$$F_i(x,Q^2) = F_i(x)$$

• Björken scaling $\rightarrow \gamma$ scatters off (charged) point-like proton constituents.





Scaling and the Quark-Parton Model

- The Quark-Parton Model (QPM) was developed by Feynman to account for scaling.
- The Proton constituents are called partons.
- Björken scaling $\rightarrow \gamma$ scatters off (charged) pointlike proton constituent.
- Partons are **Quasi-free**, and regarded as being independent over the time of collisions.
- Deep Inelastic Scattering (DIS) takes place in the QPM as single photon exchange between the incoming electron and a parton.
- F_1 , F_2 measure the momentum distribution of the charged partons within the proton in terms of x (momentum fraction of proton).
- Parton Model predicts scaling.



The Quark Parton Model I

- Successes:
 - Provides a method to deal with strong interactions by focusing on their effect on parton distributions.
 - With parton distributions, electron-hadron processes became calculable in terms of first order QED processes.
- Questions:
 - What are the partons? Are they Quarks?
 - Partons must be Quasi-free to account for scaling, but constituent quark model requires strong inter-quark forces.
- Need an extra QPM assumption to stop quarks flying out of the proton after scattering. (No quarks observed in remnants of collisions).
- Feynman showed that scaling would be observed in DIS irrespective of parton nature.

The Quark Parton Model II

- Subsequent work focused on the attributes of partons.
- We can express the contribution of each quark to F_i using the fact that the interactions are from QED:

$$F_2(x) = \mathop{\scriptscriptstyle \sum}_{q,\bar{q}} e_q^2 x q(x)$$

Where q(x) is the probability of finding a parton with momentum fraction between q and q + dx

- Relative magnitudes of F_1 and F_2 are determined by spin.
- $R = F_1 2xF_1$ was measured as approximately 0 (Callan-Gross relation), as would be expected in the spin $\frac{1}{2}$ case.
- 3 quark (uud) model of protons overestimated the measured size of the structure functions by approximately 2.
- Break down quark component into:
 - "Valence" component: comprising minimum SU(3) composition of the hadron.
 - "Sea" component: SU(3) singlet cloud containing indefinite number of quarks.

Sea Quarks and Sum Rules

- When probed at a scale Q^2 , the sea contains all flavours with $M \ll Q$.
- at $Q \approx 1 GeV$ appropriate pdf's are:

$$u(x) = u_V x + u_S(x), u(x) = d_V x + d_S(x), s(x) = s_S(x)$$

expect that $\bar{u}(x)=\bar{d}(x)=s(x)=\bar{s}(x)$

• Expect the proton momentum sum rules, to hold:

$$\int_{0}^{1} u_{V}(x) \, \mathrm{d}x = 2 \text{ and } \int_{0}^{1} d_{V}(x) \, \mathrm{d}x = 1$$

• It was measured that:

$$\sum_{q} \int_{0}^{1} q(x) + \bar{q}(x) \sim 0.5$$

• 50% of proton momentum is not carried by quarks.

Gluons and QPM

- Other 50 % of proton momentum must be carried by neutral particles.
- Natural solution: neutral boson exchanged by quarks in strong interactions.
- QPM modified to include a nuclear glue-particle responsible for the inter-quark force: The Gluon
- Inclusion of a gluonic component reduced structure functions, improving description of the SLAC data.

Strong Interactions and QFT

- In QFT no realistic interacting theory existed predicting scaling.
- The success of the parton model and scaling phenomena in DIS was explained with the demonstration of the asymptotic freedom property of gauge theories.
- Gauge theories are invariant under local transformations of the fields and thus the predictions of the theory are unchanged by such transformations.
- Asymptotic freedom means that at high momenta gauge theories behave as free, non-interacting field theories.
- *important steps:*
 - 1972: Gross and Coleman demonstrate that no renormalisable field theory except gauge theories, could account for scaling.
 - 1973: Politzer and Wilczek demonstrate asymptotic freedom of gauge theories.
 - 1973: Gross and Coleman demonstrate that no theory without gauge fileds asymptotically free.
- A field theory of the strong interaction must be a gauge theory.

QCD: A Gauge Theory of the Strong Interaction.

- Assume that the fundamental gauge fields are the quarks interacting via the exchange of gauge vector fields (gluons).
- since quarks are fermions, the total wave function must be antisymmetric under quarkinterchange. Wave functions of quarks were represented by three components.

 $\Psi_q = \psi_{SU(3)_F} \phi_{\rm spin} \psi_{\rm space}$

Which is symmetric overall under exchange of quarks.

- Solution : Introduce a new Quantum number \rightarrow **Colour**
- Hence the gauge theory of strong interactions describing the strong interactions between quarks and gluons within the SU(3) group of colour is known as Quantum Chromo Dynamics (QCD).
- 3 Colour charges, conserved at each vertex, are used:

 quarks are singly charged.
 gluons doubly charged.

QCD and Confinement

- QCD exhibits the two most important properties of quark and gluon interactions: aymptotic freedom and confinement.
- Confinement offers a solution to the problem of the lack of observation of free quarks.
- Since gluons also carry colour charge, they can couple directly to other gluons.
- The potential energy required to separate quarks increase linearly with their distance.



- Quarks and gluons are only seen in colourless hadrons.
- Large amounts of energy to break up hadrons.
- This energy is needed to create quark-anti-quark pairs.

Asymptotic Freedom

• In QFT a quark can emit a gluon, the gluon can decay to a $q\bar{q}$ pair and so on.



• The $\bar{q}q$ pairs surround the quark and diffuse the effective colour of the quark.

Asymptotic Freedom

- A red charge for example is surrounded by a cloud of colour dipoles antiscreening the colour charge.
- To determine the charge, measure the force experienced by a test charge.
- moving the test charge towards the quark leads to decrease in measured charge!
- This antiscreening results in asymptotic freedom.
- When very close together, the quarks interact through colour fields of reduced strength, and behave as free non-interacting particles.



α_S the QCD Coupling Constant

- α is a measure of the strength of the EM interaction. $\alpha = \frac{e^2}{4\pi}$
- In QED, α gives the probability of emitting a photon.



- a factor $\sqrt{\alpha}$ is associated with each absorption or emission of a photon by a charge *e*.
- α_S is the QCD analogue to α : $\alpha_S = \frac{g_S^2}{4\pi}$ where g_S is the colour charge.
- In QCD, α_S gives the probability of emitting a gluon.



• a factor $\sqrt{\alpha_S}$ is associated with each absorption or emission of a gluon by a colour charge g_S .

Running of Coupling Constants



- In QED the electric charge seen depends on the distance from the particle, due to screening. α depends on the scale, and is said to run.
- In QCD the magnitude of the strength also depends on the scale at which we view the particle. So α_S also runs.
- In QCD the value of α_S is small at short distances, this is the scale at which perturbation theory works.

Grand Unification

- We expect all couplings to merge at a very large (10^{15} GeV) energy scale.
- At this stage a Grand Unification theory (GUT) would unify the strong, weak and EM interactions, making them all aspects of the same interaction.
- Several models have been proposed, none are entirely satisfactory, so far.
- GUT's predict lifetime of 10^{31} years for the proton.
- Hitherto there has been no detection of proton decay, (but nice results on neutrino mass!)



Can QCD Account for Strong Interactions?

- To test the validity of any theory, it's predictions must confront experimental data. Important predictions:
 - 3 Colour States per Quark: Cross sections should yield evidence that there are 3 colour degrees of freedom for each quark in a final state.
 - Scaling Violations: With increasing Q^2 , $F_2(x, Q^2)$ should increase at small x and decrease at large x.
 - **Running of** α_S : α_S should decrease with increasing Q^2 .
 - Hadronic Jets: Since quarks and gluons cannot be seen in isolation, we should only directly observe hadronic jets.
 - Gluon Jets: Some jets should originate from gluons.
 - *Gluon Self Coupling*: Evidence for a ggg vertex should be observed.

Measuring Quark Colour Species

$$\sigma(e^+e^- \to \mu^+\mu^-) = \frac{4\pi\alpha^2}{3s}, \ \sigma(e^+e^- \to q\bar{q}) = n_c \mathop{\scriptstyle \Sigma}_q e_q^2 \frac{4\pi\alpha^2}{3s}$$

- Expect $R = \frac{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}{\sigma(e^+e^- \rightarrow q\bar{q})} = n_c \sum_q e_q^2$
- Well measured muonic cross section makes it possible to confirm number, colour states and electromagnetic charge of quarks.
- R=2(u, d, s), 10/3(u, d, s, c), 11/3(u, d, s, c, b), 15.3(u, d, s, c, b, t), $n_c=3$



Scaling Violation

- The QPM predicts exact scaling.
- *QCD* predicts that exact scaling is broken by:



Gluon emission by a quark (QCD compton process)



DIS with initial gluons (Boson-Gluon Fusion Process).

- These give rise to terms $\propto \alpha_S \ln Q^2$ which break scaling.
- Such logarithmic scaling violations are a property of gauge theories with point like fermion-vector boson couplings.

Scaling Violation

• QCD gives the quark parton distribution in the proton to $\mathcal{O}(\alpha_S)$ as:

$$q(x,Q^2) = q_0(x) + \frac{\alpha_S}{2\pi} \left\{ q_0(x) \otimes P_{qq}(x) \ln \frac{Q^2}{\kappa^2} + g_0(x) \otimes P_{qg}(x) \ln \frac{Q^2}{\kappa^2} \right\}$$

where P_{ij} are the splitting functions.

• The Q^2 evolution of $q(x,Q^2)$ is governed by the DGLAP evolution equations.

$$\begin{aligned} \frac{\partial q_{NS}}{\partial \ln Q^2} &= \frac{\alpha_S(Q^2)}{2\pi} P_{qq}^{NS} \otimes q_{NS}, \\ \frac{\partial}{\partial \ln Q^2} \begin{pmatrix} q_S(x, Q^2) \\ g(x, Q^2) \end{pmatrix} &= \frac{\alpha_S(Q^2)}{2\pi} \begin{pmatrix} P_{qq} & P_{qg} \\ P_{gq} & P_{gg} \end{pmatrix} \otimes \begin{pmatrix} q_S(x, Q^2) \\ g(x, Q^2) \end{pmatrix}, \\ q_S &= q + \bar{q}, q_S = q - \bar{q} \end{aligned}$$

• Solutions mean that as Q^2 increases the NS distribution function decreases at large x and increases at small x, so that the phase space for gluon emission by quarks increases as Q^2 increases.

Experimental Evidence for Scaling Violation



Plot showing measurements of $F_2(x, Q^2)$ in DIS from collider (ZEUS) and fixed target (E666,NMC,BCDMS) experiments.

Here we see that F_2 is increasing with Q^2 for small x and decreasing at large x.

Note the large increase in Q^2 and x ranges due to the HERA experiment.

Running of α_S

• The magnitude of the colour charge is modified by antiscreening.



- The sum of a geometric series giving $g_S^2 = g_{S_0}^2 \left(\frac{1}{1+I(Q^2)}\right)$
- We expect that α_S will run with Q^2 .

Running of α_S

- For QCD, $I(Q^2) = \frac{\alpha_S(\mu^2)}{12\pi} (33 2N_F) \ln \frac{Q^2}{\mu^2}$, (μ is a reference scale)
- At sufficiently low Q^2 , the effective coupling becomes large. The scale at which this happens is $\Lambda^2 = \mu^2 \exp\left[\frac{-12\pi}{(33-2N_F)\alpha_S(\mu^2)}\right]$
- Then: $\alpha_S(Q^2) = \frac{12\pi}{(33-2N_F)\ln\frac{Q^2}{\mu^2}}$
- $\alpha_S(Q^2)$ decreases with increasing Q^2 and is small for short distance interactions.
- for $Q^2 \gg \Lambda^2$, perturbative description in terms of quarks and gluons interacting weakly is possible.
- for $Q^2 \approx \Lambda^2$, the quarks and gluons are tightly bound in hadronic states and perturbation theory is inapplicable.
- The important parameter Λ is not predicted by theory and must be determined by experiment. Recent measurements give $\Lambda = 208^{+25}_{-23}$ MeV.

Running of α_S

 α_S from jet rates in DIS at HERA:



The fraction of DIS events containing 2 jets relative to the fraction containing 1 jet is proportional to α_S .

$$\alpha_S(M_Z) = 0.1166 \pm 0.0019 (\text{Stat}) {}^{+0.0024}_{-0.0033} (\text{Exp}) {}^{+0.0057}_{-0.0044} (\text{Theo})$$

Jets

- Quarks and Gluons cannot be observed directly.
- The collision of very high energy electon + positron beams offers an opportunity to look for direct evidence for quarks.
- Photons are produced in e^+e^- collisions.
- Can produce $q\bar{q}$
- $q\bar{q}$ pull apart producing 2 jets travelling in the same direction as the quarks and approximately opposite to each other.



Experimental Evidence For Jets

- First observation of back to back 2-jet events in $e^+e^- \rightarrow q\bar{q}$ at SPEAR in 1975.
- The collision of very high energy electon + positron beams offers an opportunity to look for direct evidence for quarks.
- Back to back collimated bunches of tracks from charged hadrons seen in the central tracking detector.
- Back to back hadronic clusters in the calorimeter.



Gluons and 3-Jet Events

- $\mathcal{O}(\alpha_S)$ correction to $e^+e^- \rightarrow q\bar{q}$ gives events with 3 jets in the final state.
- Jets are coplanar to conserve momentum.
- first direct evidence for gluons by observation of 3 jet events at PETRA in 1979.



Gluons and 3-Jet Events

- The leading order cross section: $\sigma_0(e^+e^- \rightarrow q\bar{q}) = 3e_q^2 \frac{4\pi\alpha^2}{3s}$, where s is the COM energy squared, is modified at $\mathcal{O}(\alpha_S)$ by gluon emission diagrams.
- the modified cross section is:

$$\sigma(e^+e^- \to q\bar{q}) + \sigma(e^+e^- \to q\bar{q}g) = \sigma_0(1 + \frac{\alpha_S(s)}{\pi})$$

• This can be written in terms of transverse momentum (p_T) between the q and \bar{q}

$$\frac{1}{\sigma} \frac{\mathrm{d}\sigma}{\mathrm{d}p_T} \sim \alpha_S \frac{1}{p_T^2} \ln\left(\frac{s}{4p_T^2}\right)$$

• For fixed p_T the cross section increases with increasing s.

Gluons and 3-Jet Events

- p_T is non-zero only when there is gluon-emission.
- The hadrons from one of the quarks should also have large p_T .



- Measurement of the p_T distribution w.r.t. the thrust axis of hadrons at different s at PETRA.
- For fixed p_T the distribution increases with increasing *s*.
- For *s* the distribution falls with increasing p_T .

Triple Gluon Vertex

- QCD is based on the non-abelian SU(3) group which introduces self-coupling of the bosons. QED is based on a non-abelian group U(1).
- Due to the gluon self-coupling, the ggg vertex should be observed in events containing at least 4 jets in the final state.
- Diagrams contributing to σ for four jet events:

abelian-like diagrams non-abelian like diagrams

Triple Gluon Vertex

- Four-jet events have been observed at LEP.
- Variables have been devised to highlight the nonabelian nature of QCD in contrast to abelian theories such as the $[U(1)]^3$ group.
- These variables are:
 - Bengtsson-Zerwas angle χ_{BZ} the angle between \mathfrak{F} the planes defined by the two lowest and two highest energy jets.
 - Nachtmann-Reiter angle θ_{NR}^* the angle between the momentum vector of the differences of jets 1,2 and jets 3,4.
 - $alpha_{34}$ the angle between the two lowest energy jets.
- these variables have been measured at LEP.
- The data clearly favours a non-abelian theory.



Colour Factors

- The dynamics of any gauge theory are completely defined by the commutation relations between its group generators Tⁱ, [Tⁱ, T^j] = i ∑ f^{ijk}T^k
- In perturbative calculations the average and sum over all possible colour configurations in the initial and final states lead to the combinatoric factors C_A , C_F and T_F .

$$\sum_{k,\eta} T^k_{\alpha\eta} T^k_{\eta\beta} = \delta_{\alpha\beta} C_F, \quad \sum_{\alpha,\beta} T^m_{\alpha\beta} T^n_{\beta\alpha} = \delta^{mn} T_F, \quad \sum_{j,k} f^{jkm} f^{jkn} = \delta^{mn} C_A$$

- C_A, C_F and T_F are known as the colour factors and are the physical manifestations of the underlying group structure.
- in QCD they represent the relative strength of the processes $q \to qg$, $g \to gg$ and $g \to q\bar{q}$
- Simulataneous measurement of C_A/C_F and T_F/C_F at in e^+e^- collisions has been made.

Colour Factors

• Predictions:

Group	C_A/C_F	T_F/C_F
SU(3)	9/4	3/8
$[U(1)]^3$	0	3
SO(3)	1	1

• Measured values are:

 $C_A/C_F = 2.11 \pm 0.16(\text{St.}) \pm 0.28 \text{ (Sy.)}$ $T_F/C_F = 0.40 \pm 0.11(\text{St.}) \pm 0.14 \text{ (St.)}$

• *SU*(3) is clearly favoured



Lecture I - Summary

- *QCD* is a well established theory of the strong interaction.
- It explained many known features of the strong interaction.
- Many predictions were made and have been confirmed by experiment.
- Nobel Prize in Physics 2004: Gross, Politzer, Wilczek

"For the discovery of asymptotic freedom in the theory of the strong interaction"